

How do I perform a Partial F-Test in Excel?

Authored by
stats writer

April 28, 2024

RECOMMENDED CITATION

stats writer (2024). *How do I perform a Partial F-Test in Excel?*. PSYCHOLOGICAL SCALES. Retrieved from <https://scales.arabpsychology.com/?p=140672>

A Partial F-Test in Excel is a statistical tool used to compare the significance of two regression models. It helps determine if adding a new variable to a model significantly improves its predictive power. This test can be performed by using the built-in Analysis ToolPak add-in in Excel. First, select the data and go to the Data tab, then click on "Data Analysis" and choose "Anova: Two-Factor with Replication" from the list. Next, select the variables for the "Model" and "Residual" fields and click "OK" to generate the results, including the F-statistic and p-value. A low p-value indicates that the new variable has a significant impact on the model's performance. This test is useful in evaluating the necessity of adding new variables to a model and making informed decisions in data analysis.

Perform a Partial F-Test in Excel

A is used to determine whether or not there is a statistically significant difference between a regression model and some nested version of the same model.

A *nested* model is simply one that contains a subset of the predictor variables in the overall regression model.

For example, suppose we have the following regression model with four predictor variables:

$$Y = \beta_0 + \beta_1x_1 + \beta_2x_2 + \beta_3x_3 + \beta_4x_4 + \varepsilon$$

One example of a nested model would be the following model with only two of the original predictor variables:

$$Y = \beta_0 + \beta_1x_1 + \beta_2x_2 + \varepsilon$$

To determine if these two models are significantly different, we can perform a partial F-test, which calculates the following F test statistic:

$$F = ((RSS_{reduced} - RSS_{full})/p) / (RSS_{full}/(n-k))$$

where:

RSS_{reduced}: The residual sum of squares of the reduced (i.e. "nested") model.
RSS_{full}: The residual sum of squares of the full model.
p: The number of predictors removed from the full model.
n: The total observations in the dataset.
k: The number of coefficients (including the intercept) in the full model.

This test uses the following null and alternative :

H₀: All coefficients removed from the full model are zero.

H_A: At least one of the coefficients removed from the full model is non-zero.

If the corresponding to the F test-statistic is below a certain significance level (e.g. 0.05), then we can reject the null hypothesis and conclude that at least one of the

coefficients removed from the full model is significant.

The following example shows how to perform a partial F-test in Excel.

Example: Partial F-Test in Excel

Suppose we have the following dataset in Excel:

	A	B	C	D	E	F	G
1	x1	x2	x3	x4	y		
2	1	15	23	19	18		
3	3	14	25	19	20		
4	3	15	24	17	24		
5	4	12	24	17	24		
6	4	10	14	15	23		
7	5	9	9	18	26		
8	7	6	17	15	29		
9	8	7	17	13	30		
10	8	5	4	19	37		
11	9	4	13	8	34		
12	10	4	6	8	38		
13	12	3	8	17	40		
14							
15							
16							
17							
18							
19							
20							
21							
22							

Suppose we would like to determine if there is a difference between the following two regression models:

Full Model: $y = \beta_0 + \beta_1x_1 + \beta_2x_2 + \beta_3x_3 + \beta_4x_4$

Reduced Model: $y = \beta_0 + \beta_1x_1 + \beta_2x_2$

We can proceed to perform for each model to get the following output:

G	H	I	J	K	L	M
Full Model	ANOVA					
		<i>df</i>	<i>SS</i>	<i>MS</i>	<i>F</i>	<i>Significance F</i>
	Regression	4	561.6047	140.4012	38.82785	7.24E-05
	Residual	7	25.31194	3.615992		
	Total	11	586.9167			
		<i>Coefficients</i>	<i>Standard Error</i>	<i>t Stat</i>	<i>P-value</i>	<i>Lower 95% t</i>
	Intercept	14.34009	7.565093	1.89556	0.099856	-3.54851
	x1	2.290687	0.59909	3.82361	0.006512	0.874064
	x2	0.516173	0.567794	0.909086	0.393528	-0.82645
	x3	-0.29052	0.153701	-1.89018	0.100649	-0.65397
	x4	0.006391	0.189974	0.033642	0.974102	-0.44283
	SUMMARY OUTPUT					
	<i>Regression Statistics</i>					
	Multiple R	0.965112				
	R Square	0.931441				
	Adjusted R	0.916206				
	Standard Error	2.114459				
	Observations	12				
Reduced Model	ANOVA					
		<i>df</i>	<i>SS</i>	<i>MS</i>	<i>F</i>	<i>Significance F</i>
	Regression	2	546.6782	273.3391	61.13686	5.78E-06
	Residual	9	40.23844	4.470938		
	Total	11	586.9167			
		<i>Coefficients</i>	<i>Standard Error</i>	<i>t Stat</i>	<i>P-value</i>	<i>Lower 95% t</i>
	Intercept	17.50073	7.99721	2.188354	0.056401	-0.59022
	x1	1.965388	0.640132	3.070286	0.013348	0.517309
	x2	-0.11969	0.475321	-0.2518	0.806849	-1.19494

We can then use the following formula to calculate the F

test-statistic for the partial F-test:

G	H	I	J	K	L	M	N	O	P	Q	R	S
Full Model	ANOVA								F test statistic	2.064	=(J12-J34)/2/K13	
		<i>df</i>	<i>SS</i>	<i>MS</i>	<i>F</i>	<i>Significance F</i>						
	Regression	4	561.6047	140.4012	38.82785	7.24E-05						
	Residual	7	25.31194	3.615992								
	Total	11	586.9167									
		<i>Coefficients</i>	<i>Standard Error</i>	<i>t Stat</i>	<i>P-value</i>	<i>Lower 95%</i>	<i>Upper 95%</i>	<i>Lower 95.0%</i>	<i>Upper 95.0%</i>			
	Intercept	14.34009	7.565093	1.89556	0.099856	-3.54851	32.22869	-3.54851	32.22869351			
	x1	2.290687	0.59909	3.82361	0.006512	0.874064	3.70731	0.874064	3.707309921			
	x2	0.516173	0.567794	0.909086	0.393528	-0.82645	1.858791	-0.82645	1.858791347			
	x3	-0.29052	0.153701	-1.89018	0.100649	-0.65397	0.072923	-0.65397	0.072923129			
	x4	0.006391	0.189974	0.033642	0.974102	-0.44283	0.455609	-0.44283	0.45560912			
	SUMMARY OUTPUT											
	<i>Regression Statistics</i>											
	Multiple R	0.965112										
	R Square	0.931441										
	Adjusted R	0.916206										
	Standard E	2.114459										
	Observatio	12										
Reduced Model	ANOVA											
		<i>df</i>	<i>SS</i>	<i>MS</i>	<i>F</i>	<i>Significance F</i>						
	Regression	2	546.6782	273.3391	61.13686	5.78E-06						
	Residual	9	40.23844	4.470938								
	Total	11	586.9167									

The test statistic turns out to be 2.064.

We can then use the following formula to calculate the corresponding p-value:

